Instability, self-organization and pattern formation in thin soft films

Rabibrata Mukherjee* and Ashutosh Sharma*

The free surface of a thin soft polymer film is often found to become unstable and self-organizes into various meso-scale structures. In this article we classify the instability of a thin polymer film into three broad categories, which are: category 1: instability of an ultra-thin (<100 nm) viscous film engendered by amplification of thermally excited surface capillary waves due to interfacial dispersive van der Waals forces; category 2: instability arising from the attractive inter-surface interactions between the free surface of a soft film exhibiting room temperature elasticity and another rigid surface in its contact proximity; and category 3: instability caused by an externally applied field such as an electric field or a thermal gradient, observed in both viscous and elastic films. We review the salient features of each instability class and highlight how characteristic length scales, feature morphologies, evolution pathways, etc. depend on initial properties such as film thickness, visco-elasticity (rheology), residual stress, and film preparation conditions. We emphasize various possible strategies for aligning and ordering of the otherwise isotropic structures by combining the essential concepts of bottom-up and top-down approaches. A perspective, including a possible future direction of research, novelty and limitations of the methods, particularly in comparison to the existing patterning techniques, is also presented for each setting.

1. Introduction

Polymer thin films are ubiquitous in many applications like optoelectronics, biotechnology, nanolithography, sensors and actuators, microfluidics, functional coatings and lubricants. A highly confined thin film is often away from thermodynamic...
equilibrium and as a result, it evolves into a lower energy configuration by spontaneous morphological transformation from an initially flat film to a micro/nano-structured morphology, including possible disintegration of the film.\(^8\) We refer to the shaping of an initially featureless film due to such instabilities, which can be spontaneous or can be mediated by an externally imposed force field as self-organization.\(^8\) This is clearly distinct from self-assembly,\(^9,10\) where a large number of molecules/small building blocks come together and assemble in an ordered fashion to form a larger supra-molecular assembly. In contrast, self-organization involves a spontaneous change of shape from a simple to a more complex organization. For example, a thin film spontaneously fragmenting into an array of holes or droplets due to instability is opposite of the self-assembly, though minimization of the free energy remains the key driving force in both the cases. It thus becomes important to understand the underlying science of thin film instability.\(^11-27\) so that ultra-thin defect free, stable coatings can be engineered in some applications and in others, the morphology of the self-organized patterns can be controlled to achieve desired surface topography and functionality, particularly in functional coatings that regulate wetting (super-hydrophobic/oleophobic),\(^28\) adhesion and friction,\(^29\) and colors,\(^30\) among many other interfacial properties and interactions.

Initial research on instability and meso-mechanics of soft thin films has evolved along two distinct paths: (a) studies involving a purely viscous liquid thin film, either free or supported on a solid substrate (wetting film), and (b) a soft, purely elastic film sandwiched between two rigid substrates, which is a special case of the adhesive film. If the film is very thin (\(<100\) nm), excess van der Waals force and other inter-surface interactions can destabilize the film. An externally applied force field such as an electric field or a thermal gradient can also destabilize both types of films. To facilitate discussion, we classify possible instabilities of a thin polymer film into three broad categories based on the nature of the confining field. Category 1: instability in ultra-thin wetting films engendered by interfacial nonpolar van der Waals and other polar interactions, leading to spontaneous rupture and dewetting of viscous and viscoelastic films.\(^31-295\) Category 2: instability triggered by inter-surface adhesive interaction between the film and a contacting surface, observed mostly in soft elastic films.\(^296-352\) Category 3: instability engendered by an external field such as an electric field or a thermal gradient, observed in both viscous and elastic films.\(^353-396\) In the case of category 1 instability, the destabilizing inter-surface interactions decrease rapidly with increase in the film thickness (\(h\)), and therefore relatively thicker films (\(h\) \(<\) few tens of nm) rupture only by nucleation around physico-chemical defects. Category 1 instability has a long-wave character (\(\lambda \gg h\)) and its growth is associated with flow of liquid from thinner to thicker, intact parts of the film.\(^6,8,58-148\) In contrast, there is no convective material transport in the case of contact proximity induced category 2 instability observed in a soft solid film. In this case, elastic deformation of the film surface results in short-wave contact instability (\(\lambda \approx 3h\)) due to minimization of elastic strain energy.\(^303-310\)

It is well known that in many nonlinear and complex systems, the equilibrium state is often not unique and there can be several metastable states corresponding to local energy minima.\(^6,58\) This particular aspect of freezing the patterns at any intermediate stage allows potential engineering of many distinct structures in the same system, which is a distinct advantage over conventional soft lithography based replication techniques widely used for nano-patterning in soft materials. The possibility of aligning and ordering the intrinsically isotropic instability patterns by a creative combination of the top down and bottom up approaches has also received significant research attention, across all instability categories.

In what follows, we present a consolidated and detailed review of various types of instabilities and pattern formation in soft thin films, without any phase change. The review mostly focuses on experimental findings, though the essential theoretical concepts are also included for completeness. The article is organized according to the different categories of instability classes. As several reviews on category 1 instability involving dewetting are already available,\(^31-47\) we discuss this section rather briefly and focus more on categories 2 and 3, which lack extended reviews.

2. Category 1: spontaneous rupture and dewetting of thin polymer films

2.1 Dewetting of thin liquid films: basic theory and mechanism

Coating techniques such as spin and dip coating of polymer solutions are commonly used to create a thin polymer film on a solid substrate regardless of its wettability, and this allows obtaining an initially intact, flat film on a non-wettable substrate which is thermodynamically unstable. Enhanced chain mobility above the glass transition temperature of the constituent polymer allows the growth of surface instability leading to increasing deformation and even disintegration of such a film.\(^49-83\) While relatively thicker films (\(h\) \(<\) few hundreds of nm) are stabilized due to gravity, the issue of spontaneous film rupture becomes unavoidable in films thinner than about 100 nm, where the stability is strongly influenced by the integrated intermolecular forces across the film.\(^73,74,82\) The linearized Navier Stokes equation for a non-slipping, isothermal, single component, Newtonian liquid film without evaporation/condensation, incorporating the influence of intermolecular forces and simplified in the lubrication approximation (negligible inertial effects), on a physically or chemically structured substrate exhibiting long-wave instability (\(\lambda \gg h\)), which captures the dynamics and evolution of a non-wettable thin film rather accurately is given as:\(^72,99,100,395,338-242\)

\[
3\mu h_{t} + [(h - a_{f})^{3} \phi_{c}(h_{c} + h_{y}) - \phi_{x}]_{t} + [(h - a_{f})^{3} \phi_{c}(h_{c} + h_{y}) - \phi_{y}]_{y} = 0
\]

where subscripts denote partial derivatives; \(h = h(x,y,t)\) is the local film thickness; \(\phi\) is the effective interface potential per unit volume (\(\phi = \partial G/\partial h\)), which is also referred to as the conjoining pressure (and \(-\phi\) as the disjoining pressure), \(G\) is the excess interaction energy per unit area which depends on
the local thickness. The term \( z = a f(x,y) \) quantifies the physical roughness of the substrate, and \( a = 0 \) for a smooth, homogeneous substrate. On a physico-chemically rough (patterned) substrate the functional form of the term \( \phi_x \) based on linearization is:

\[
\phi_x = [\partial \phi / \partial h](\partial h / \partial x) + (\partial \phi / \partial x) \left|_h \right.
\]

(2)

The second term represents the in-plane potential gradient due to substrate non-homogeneity and vanishes on a homogeneous substrate. Eqn (1) is extensively used in assessing the stability of an initially uniform film of mean thickness \( h_0 \).\textsuperscript{72} The stability of a film is tested using this equation by checking the response of the free surface to a periodic small amplitude perturbation \( (\varepsilon \ll h_0) \) of wavenumber \( k \), of the form:

\[
h(x,t) = h_0 + \varepsilon \sin(kx) \exp(\omega t)
\]

(3)

where \( \omega \) is the initial growth coefficient. From linear stability analysis, it is possible to obtain:

\[
\omega = C [ - \gamma k^4 - (\partial \phi / \partial h) k^2 ]
\]

(4)

From eqn (3), it can be clearly understood that for the perturbation to grow with time, \( \omega \) must be positive. This becomes possible only when \( \partial \phi / \partial h < 0 \), as the first term in eqn (4), which represents that the effect of surface tension is always negative and therefore has an unconditional stabilizing effect.\textsuperscript{72} Thus, a film can be distinguished when \( (\partial \phi / \partial h) < 0 \) for all \( h \); unstable \( (\partial \phi / \partial h < 0) \) and metastable \( (\partial \phi / \partial h > 0) \) only up to a certain specific value of \( h \) and \( \partial \phi / \partial h < 0 \) beyond \( h > h_c \).\textsuperscript{62,72,73,99,105} Metastable films rupture due to finite amplitude thermal fluctuation at the surface or by nucleation around a defect, where the local film thickness is often lower. When \( \partial \phi / \partial h < 0 \), the growth of instability is spontaneous and is referred to as spinodal dewetting due to its similarity to the well-known spinodal decomposition in fluid mixtures. The term \( \partial \phi / \partial h \) is referred to as the spinodal parameter as it plays the same role as the effective diffusivity in the phase separating mechanisms to remove any possible nonphysical singularity at rupture.\textsuperscript{117} The third Born repulsion term is included in simulations to account for any acid–base (AB) type interactions in a polar liquid like water (hydrophobic repulsion) as well as the entropic confinement effects due to adsorption/grafting of polymer brushes at the film–substrate interface. The third Born repulsion term is included in simulations to remove any possible nonphysical singularity at rupture as \( h \to 0.72\textsuperscript{72} 

Fig. 1 (A) Indicative \( \phi \) vs. \( h \) plots for a spinodally unstable (line 1), stable (line 2) and metastable (line 3) film respectively. The metastable film is stable for \( h > h_c \) and unstable for \( h < h_c \). (B) A typical LSA result showing the formation of 9 holes on a \( 10 \times 10 \) domain for a 5.5 nm thick film for which \( h_c = 6.8 \) nm. (C) Time evolution \((c_1 \to c_4)\) of instability in a 5.5 nm film on a \( 10 \times 10 \) domain, based on non-linear simulations starting with a random roughness of 1% maximum amplitude at the initial time. The images correspond to \( t = 0.933, 0.992, 1.060 \) and 1.129 respectively, where \( t \) is calculated from eqn (5C). (B and C) Reproduced with permission from ref. 72. Copyright 2003, European Physical Society.

Interactions are the long range a-polar van der Waals force and shorter range polar interactions.\textsuperscript{72,73,85} It is important to point out that no instability is possible in the absence of an interfacial attraction, as any long range interfacial repulsion would stabilize the film (curve 2, Fig. 1A). A popular representation of \( \phi \) for an unstructured thin liquid film that works rather well for a variety of materials including polymers is: \textsuperscript{72}

\[
\phi = (A_S / \pi \hbar^4) - (S_p / \pi \hbar^2) \exp(-h/\hbar) - (B/\hbar^3)
\]

(6)

where \( A_S \) refers to the effective Hamaker constant for van der Waals interaction; a positive or negative value of \( A_S \) denotes long-range attraction or repulsion, respectively. \( S_p \) denotes the strength of any medium or short-range interaction, which can be attractive \((S_p < 0)\) or repulsive \((S_p > 0)\); \( \hbar \) is the corresponding decay length. This term accounts for any acid–base (AB) type interactions in a polar liquid like water (hydrophobic repulsion) as well as the entropic confinement effects due to adsorption/grafting of polymer brushes at the film–substrate interface. The third Born repulsion term is included in simulations to remove any possible nonphysical singularity at rupture as \( h \to 0.72,72 \textsuperscript{72} 

It can be seen from eqn (6) that \( \partial \phi / \partial h = -A_s / 2 \pi \hbar^4 \) (considering only the first term). Thus, the van der Waals force is destabilizing when \( A_S \) is positive, signifying an attractive interfacial interaction.\textsuperscript{45,65–67,72,82,117} Under such a condition, the attractive interaction grows stronger with a decline in the local thickness and amplification of the thermal fluctuations at the free surface of the film. The growing amplitude eventually leads to the rupture of the film with formation of holes, which subsequently grow, coalesce with neighboring holes and eventually lead to isolated, random droplets.\textsuperscript{62,72,82} This analysis is however valid only for unstable and metastable films \((h < h_c)\).\textsuperscript{72,82} A thermodynamically stable film can also rupture due to nucleation around substrate defects or heterogeneities such as dust, trapped micro-cavities, and chemical contamination, which results in a non-zero \( (\partial \phi / \partial x) \) term in
eqn (2) even on a smooth fully wettable surface. If the in-plane potential gradient supplies adequate driving force to the liquid to flow out of the heterogeneous patches, the local h may → 0, a scenario that is known as “true” or “heterogeneous” nucleation. The same mechanism can lead to the reduction of local film thickness well below hC, in a metastable film having initial h > hC, and thus trigger instability. On the other hand, a metastable film with an initial h just above the spinodal boundary (h marginally > hC) can rupture due to “thermal” or “homogeneous” nucleation, as the term ∂φ/∂h might undergo a local reversal in sign due to fluctuations present on the free surface of the film. This regime is often referred to as the “defect sensitive spinodal regime” (DSSR), and is clearly distinct from possible nucleated rupture of a film even within the spinodal envelop. In case both the modes of instability are cooperative in a specific film, the morphological evolution is governed by the mode with a faster timescale of evolution, though the final morphology often bears the signature of both the modes in experiments. Initially, nucleation was considered to be the only mechanism possible for the rupture of stable films, which includes thick films and films on wettable substrates. However, many experiments reported dewetting of thicker thermodynamically stable films on wettable substrates, including the classic example of the extremely well investigated dewetting of a polystyrene (PS) thin film on a native oxide coated silicon wafer substrate:91–98, 101–103 Bollinne et al. reported spinodal like dewetting in 15 nm thick PS films, though they found that the temporal dependence of the wavelength of the growing instability did not fully agree with the classical theory of spinodal dewetting. To justify such enigmatic occurrences, as well as to account for observations such as satellite hole formation and variation of Nm, as a function of aging time, several other mechanisms like localized density variation along the film thickness, additional forces arising out of confinement of thermally excited acoustic waves, the effect of thermal noise, the influence of molecular recoiling, the effect of chain ends, the choice of solvent during coating, substrate cleaning procedures, etc. have been proposed over the years. Reiter and coworkers have shown that residual stresses generated during spin coating and subsequent film drying play a major role in dewetting in high molecular weight films beyond the chain entanglement limit. Their work show that the probability of hole nucleation reduces with longer aging and annealing, and is manifested as reduced Nm of holes in samples aged longer (for months). While linear stability analysis (LSA) is useful for assessing the stability of a film, it does not provide adequate details about the precise shape and evolution sequence of the structures and prescribes a featureless superposition of randomly oriented small amplitude waves, as can be seen in Fig. 1B. The limitation of LSA has been overcome based on full three-dimensional (3D) nonlinear simulations that predict the morphology of an evolving film during different stages, allowing direct comparison with experiments. For the simulations, eqn (1) in a non-dimensional form is discretized in space. The resultant set of coupled ordinary differential equations (ODEs) is solved as an initial value problem with a volume preserving initial random perturbation, or other forms of initial perturbations under periodic boundary conditions. A typical set of predicted morphology based on non-linear simulations is shown in Fig. 1C. Complex dewetted morphologies as well as dewetting pathways in various settings have been fully captured by 3-D simulations, and favorably compared with experimental findings. 2,51,70,73,113–115

2.2 Dewetting of thin polymer films: experiments

Experimentally, dewetting of thin polymer films has been investigated for a wide variety of materials, though dewetting of PS thin films on silicon substrate has received maximum attention, arguably due to easy availability of PS. Other polymers that have been used for dewetting experiments include poly-methylmethacrylate (PMMA), poly-dimethylsiloxane (PDMS), perfluoroalkylmethacrylate, perfluoropolyether (PFPE), polyelectrolytes, and in various liquid crystals such as CB5 and CB8. True spinodal dewetting takes place in extremely thin films (h < 5 nm) and is therefore difficult to capture, as substrate heterogeneities tend to rupture such films in most cases. The undulating, bi-continuous features in spinodal dewetting, shown in Fig. 2A was first captured by Xie et al. in a 4.5 nm thick low molecular weight PS film (Mw = 4k) on a silicon substrate. The average amplitude of undulations grows with time in spinodal dewetting, and the film eventually disintegrates into small, uniformly sized droplets. These droplets at later stages coarsen through a coalescence process (inset of Fig. 2A). Similar undulations have subsequently been captured by Herminghuas and Steiner in films of similar thickness. Seeman et al. captured clear distinction in the morphology and the dewetting pathway between spinodal, homogeneous and heterogeneous dewetting. Experiments with thicker films in many cases carry a combined signature of spinodal and nucleated dewetting, where the onset of instability is with the appearance of nearly equal sized, random holes which grow with time (Fig. 2B). A distinct rim appears around the holes just ahead of the moving contact line due to mismatch in the rates at which the polymer is dislodged from the substrate and redistributed over other intact parts of the film. The evolution of the rims, forming a network of polymer ribbons known as the cellular pattern (Fig. 2C), which subsequently break down into isolated droplets, due to Rayleigh instability.
The appearance of satellite holes around the rims of pre-existing holes leading to a hole formation cascade is often observed in nucleated dewetting. Satellite hole formation is favored by the precise profile of the rim, as they are seen to form in locations where the rim has a locally depleted shallow profile towards the intact side of the film. In films of high molecular weight polymers, the rim often exhibits secondary instability in the form of undulating fingers (Fig. 2E) and eventually disintegrates into the corona of liquid droplets along the inner perimeter of the hole on non-wettable substrates, due to Rayleigh–Plateau instability. In such a scenario, the final dewetted morphology comprises of completely random collection of droplets (Fig. 2F), rather than droplets arranged along the arms of the cellular patterns (Fig. 2D in the absence of rim instability).

Dewetting in a polymer film is typically engendered by heating the film beyond the \( T_g \) of the polymer, which results in significant reduction of viscosity. It is argued that in ultra-confined thin films, there is a potential reduction of \( T_g \) as compared to bulk, due to reduced packing density of the polymer molecules, which induces additional mobility to the molecules, and dewetting may take place even at temperatures below the bulk \( T_g \). Exposing the film to its solvent vapor is the other preferred route to initiate dewetting, where the solvent molecules penetrate into the polymer matrix and effectively lower the \( T_g \) below the room temperature. Solvent assisted dewetting has been observed during chemical vapor deposition of a polymer thin film. Xu et al. have reported a non-solvent induced dewetting of PS thin films on a hydrophilic surface at room temperature in the presence of water vapor. The water molecules penetrate into the hydrophilic substrate and dislodge the polymer molecules following a penetration-replacement mechanism.

Recently, Verma et al. reported a rapid, room temperature dewetting protocol which reduces the instability length scale by more than an order. The film is immersed in a mixture of a good solvent and a non-solvent, for example, a mixture of MEK and water for dewetting of PS and PMMA films. The good solvent selectively permeates into the film, reducing its \( T_g \) below room temperature and simultaneously lowering the stabilizing interfacial tension to nearly zero. The presence of a large amount of water (non-solvent) in the solution prevents complete dissolution of the polymer film. The presence of (polar) water additionally results in a strong destabilizing electrostatic force. A combination of all these leads to extremely fast dewetting and results in much smaller features. In particular, lower interfacial tension leads to greatly reduced lateral resolution of the droplets (down to \( \sim 40 \) nm) with about an order reduction in the periodicity of the dewetted features. The electrostatic force also alters the scaling between \( \lambda \) and \( h \) to \( \lambda \sim h^{3.5} \), in contrast to \( \lambda \sim h^3 \) (Fig. 3A), observed in the van der Waals force driven instability of a film in air. Owing to a greater propensity of wetting of the substrate by the liquid mix, the dewetted polymer structures have very high contact angles (\( \sim 140^\circ \)), allowing possible fabrication of high curvature micro/nano-lenses (Fig. 3B), which is not possible in classical dewetting where the droplet aspect ratio is invariably low as it is governed by the equilibrium contact angle between the polymer and the substrate.

### 2.3 Effect of visco-elasticity and slippage on dewetting

Films of long chain polymers beyond the entangle limit exhibit significant visco-elasticity (VE) as well as finite slippage on smooth passive surfaces. Interfacial slippage in a polymer melt is generally attributed to the adsorption of molecules on the solid surface and is characterized by a slip length \( b = \eta / \zeta \), where \( \eta = \) liquid viscosity and \( \zeta = \) coefficient of friction. With increase in shear strain, the extent of disentanglement of the...
surface adsorbed molecules increases, which rapidly reduces the interfacial friction and enhances the slippage. Significance slip-page is observed when a film dewets on a substrate covered with end-grafted polymer chains of the same polymer (autophobic dewetting), or a different one. Autophobic dewetting is driven by a finite interfacial tension between the film and the grafted layer due to entropic effects, and exhibits a slip length as high as ~10 μm. Interfacial slippage is also observed in films dewetting on self-assembled monolayer (SAM) covered substrates due to the physicochemical roughness resulting from incomplete grafting, rather than entanglement or non-wettability, as the extent of slippage reduces with enhanced graft coverage.

Reptation time \( (τ_{\text{rep}}) \) is a key parameter related to VE of a polymer as it behaves like a deformable semi-solid for \( t < τ_{\text{rep}} \) and like a liquid only when \( t > τ_{\text{rep}} \). The effect of VE is pronounced when the dewetting temperature is close to \( T_c \) of the polymer. Distinctive signatures of VE on a dewetting film, which are not observed in a purely viscous film with zero interfacial slippage are: (i) formation of holes without rims in the initial stages of rupture; (ii) variation in dewetting velocity during different stages of hole growth (Fig. 4A); (iii) formation of highly asymmetric rims (Fig. 4B); and (iv) complete inhibition of hole growth beyond a critical hole radius \( (R_c) \).

In a purely viscous film, a rim with uniform curvature appears right after rupture; a constant dewetting velocity is observed; and holes grow fully and coalesce. In a VE thin film, an exponential growth rate of the hole radius, \( R(t) = R_0 \exp(\text{t}/τ_{\text{D}}) \) is observed in the early stages of dewetting (Fig. 4A), where \( τ_{\text{D}} = 0.7(h_d/V^*) \), and \( V^* = γ/η \) is the capillary velocity, which is in contrast to a power law growth rate observed in a purely viscous film. During hole growth, the gain in the interfacial energy due to amplification of surface capillary waves is balanced by viscous dissipation which occurs both within the film and at the film–substrate interface.

In the early stages \( (t < τ_{\text{rep}}) \), the film is solid like and the amplification of the surface undulations leads to an elastic deformation of the film surface, resulting in the Laplace pressure \( (S/\hat{h}) \) at the edge of the hole. This causes the elastic stress to propagate across the film at the shear wave velocity as a long range plug flow without any localized accumulation of polymers, which manifest as holes without rims. A hole continues to grow without a rim as long as interfacial dissipation remains insignificant till \( R \) attains a critical value \( \Lambda = (h_d b)^{0.5} \). For \( R > \Lambda \) dissipation starts dominating due to enhanced interfacial friction and the elastic shear stress gets screened at a finite distance from the center of the hole, paving the way for the appearance of a rim along the hole periphery.

\[ \text{Fig. 3} \] (A) Double-logarithmic plot of wavelengths or the mean separation between holes \( (λ) \) as a function of PS film thickness for dewetting in air and in a water solvent mixture. The slope of the best fit line is 1.51 ± 0.06 in the case of the water solvent mix as opposed to 2.19 ± 0.07 for air. (B) Time evolution of contact angles of dewetted droplets of a 22 nm PS film showing large contact angles in the case of dewetting in a water solvent mixture, after: (B1) 3 min, (B2) 10 min, (c) 20 min, and (d) 1 hour. Scale bar: 500 nm. (A and B) Reproduced with permission from ref. 150. Copyright 2011, American Chemical Society. (C) Schematic of the overall dewetting behavior of a nonlinear viscoelastic polymer film along with associated rim shapes. Reproduced with permission from ref. 186. Copyright 2003, American Physical Society. (D) Anisotropic rim formed due to dewetting of a 24 nm thick visco-elastic PS film after annealing at 120 °C for 80 minutes. Scale bar is 5 μm. reproduced with permission from ref. 177. Copyright 2001, American Physical Society.

\[ \text{Fig. 4} \] (A) Influence of substrate pattern periodicity on the final morphology (aligned, partially aligned and random droplet arrays) of structures resulting from dewetting of a 12 nm thick PS film. Optical micrographs and insets show transition from the doublet state (15–12 μm stripe width), to coalescence (9 μm), confinement (6 and 3 μm), and a heterogeneous morphology (1 μm) with bridging over multiple bands. Dashed lines (insets) indicate registry with the underlying chemical pattern period. AFM images (9 and 6 μm) highlight the control of droplet size and spatial position. Reproduced with permission from ref. 233. Copyright 2002, American Chemical Society. (B) Morphology diagram for dewetting of a film on a striped surface. Broken lines, 1, 2, 3, and 4, denote the boundaries between different regimes at the onset of dewetting as shown in the figure by three symbols. The shaded region corresponds to good templating. Reproduced with permission from ref. 238. Copyright 2001, American Physical Society.
2.4 Directed dewetting under lateral confinement

Preceding discussion shows that dewetting of a thin polymer film results in random structures, irrespective of the precise rupture mechanism. In this section, we discuss how these random structures can be aligned by templating, which includes the use of a topographically or a chemically patterned substrate. Such an approach combines the essential features of top down soft lithography with bottom up self-organization. Higgins and Jones first demonstrated the possibility of anisotropic dewetting by simply rubbing the substrate in a specific direction with an emery paper before coating the film. The scratch marks guided the dewetting pathway of a PMMA film resulting in anisotropic, oriented structures. A variety of ordered structures like nano-grooves, lines, droplets, etc. have been obtained by brushing a smooth film before dewetting. Spontaneous dewetting of a PDMS film deposited by wiping it with a paper pre-soaked with dilute polymer solution in a specific direction resulted in aligned nano-channels with a periodicity as low as 16 nm. Such approaches however fail to fabricate ordered instability structures with precise control over geometry, periodicity and fidelity, in a reproducible manner. This can be achieved by dewetting a film on a chemically, or topographically patterned substrate, typically fabricated by top down lithographic techniques.

2.4.1 Dewetting on chemically patterned substrates. A chemically patterned substrate with alternate zones of less and more wettable areas acts as a closely packed array of chemical heterogeneity. For a thin film on such a surface, the term $\frac{\partial \phi}{\partial x}$ in eqn (2) becomes significant, as it triggers outward flow of a polymer from less wettable to more wettable areas of the substrate. The mechanism of flow is similar to Marangoni flow, except that the flow originates due to in-plane curvature induced surface tension. This leads to partial stabilization of an unstable thin film, as theoretically predicted by Safran and Klein. The asymmetric rim shape in a VE film is attributed to several factors such as elasticity, strain hardening, and shear thinning of the polymer melt.

2.4.2 Dewetting on topographically patterned substrates. Dewetting features can also be aligned by using a topographically patterned substrate. However, things become more complicated on such a substrate as direct spin coating on a topographically patterned substrate results in a film with an undulating top
Such a film preferentially ruptures over the areas where it is thinnest.\textsuperscript{247,248} On a topographically patterned substrate even the molecular weight and the radius of gyration ($R_g$) of the polymer influence the stability of the film. These et al. showed that a film becomes unstable only when the thickness of the thinnest part of the film is below a critical thickness $t_{\text{Peak}}$, which varies as $t_{\text{Peak}} \approx 0.55R_g$ for a PS film.\textsuperscript{252} On the other hand, if the concentration of the polymer in the dispersed drop is extremely low, the film ruptures and dewets during the spin coating process itself, which is later being referred to as spin dewetting and can result in well aligned structures on a topographically patterned substrate.\textsuperscript{250,251}

Recently an alternating droplet array of PS and PMMA has been realized based on sequential spin dewetting of the two polymer solutions on a grating patterned substrate, which can be seen in Fig. 5A.\textsuperscript{251}

Instead of directly spin coating the film on a topographically patterned substrate, in some cases a flat film of uniform $h$ has been transferred on to a patterned substrate by floating.\textsuperscript{90,255} In such cases, the dewetting pathway is strongly influenced by the nature of initial adhesion of the transferred film with respect to the substrate as two distinct initial configurations are possible: (1) conformal adhesion: when the film adheres closely to the contours of the substrate pattern (inset B1, Fig. 5B) and (2) focal adhesion: in this case the film is in contact only with the protrusions of the substrate (inset C1, Fig. 5C).\textsuperscript{90,255} A film in focal adhesion upon dewetting on a patterned substrate comprising an array of square pillars results in an array of droplets that occupy the interstitial places surrounding each pillar (Fig. 5B). In contrast, the droplets get positioned on top of the pillars in dewetting of a focally adhering film (Fig. 5C).\textsuperscript{90} On a 2-D patterned substrate, perfect ordering occurs only over a narrow film thickness range.\textsuperscript{90} Dewetting of polymer films on patterned surfaces with various other geometries has also been investigated.\textsuperscript{251–263} Roy et al. showed that the extent of ordering as well as the evolution pathway depends strongly on the height of the substrate features. In case the as-cast film is continuous and thick, then even on a patterned substrate the film ruptures due to nucleation of random holes uncorrelated to the substrate patterns.\textsuperscript{259} A very recent paper reveals the possibility of obtaining aligned and ordered features from dewetting of a pre-patterned film on a template free, flat substrate when the remnant thickness at the valleys of the film after patterning is adequately low, so that the film preferentially ruptures over these locations ahead of surface tension induced flattening known as slumping.\textsuperscript{261} Ordered dewetted patterns on topographically patterned substrates have been utilized for fabricating polymer thin film transistors, optical memory, and functional devices.\textsuperscript{47,262,263}

2.5 Dewetting of a thin polymer bilayer

Dewetting of a polymer bilayer is more complicated as it involves coupled evolution of two deformable interfaces.\textsuperscript{264–295} Instability of a bilayer may either involve dewetting of a thin polymer film on a thick, viscous stable bottom layer,\textsuperscript{264–273} or both the layers can become unstable sequentially.\textsuperscript{274–288} The final dewetted droplet geometry over a non-wetting soft bottom layer is given by the well-known Neumann configuration, instead of Young’s configuration, which specifies the drop shape over a solid substrate.\textsuperscript{264,265} In case the viscosity vis-a-vis the molecular weight of the bottom layer is high, then the system behaves identical to dewetting of a thin film on a rigid substrate. Brochard and coworkers, based on detailed theoretical analysis on dewetting and stability of a liquid bilayer, have identified the existence of two collective modes of deformation in a stratified system, which are: (1) a transverse bending mode that is associated with vertical displacements, governed by the total surface tension; and (2) a longitudinal peristaltic mode which is associated with thickness fluctuations and horizontal displacements.\textsuperscript{264,265,286–288} It is also argued that in a low viscosity bottom layer, a visco-inertial mode becomes dominant.\textsuperscript{264} In case the bottom layer has viscosity comparable or lower than that of the dewetting top layer, then the rims formed around the holes penetrate into the bottom layer as a result of the vertical component of interfacial energy exerted on the soft substrate along the contact line, resulting in a rim profile that is highly asymmetric with a steep decay inside the hole.\textsuperscript{267} Faldi et al. reported that during dewetting of a polycarbonate film on a 200 nm thick styrene-co-acrylonitrile (SAN) layer, polymer from
under the layer gets pulled into the rim and lowers the film thickness of the intact bottom layer within the hole. 266 Sferrazza et al. studied the early stages of evolution of a PMMA–PS bilayer coated on a silicon substrate using specular and off-specular neutron reflection and clearly observed the amplification of the thermally excited capillary waves at the polymer/polymer interface. 270 During dewetting of a PBrS film on a PS layer, Slep et al. showed that the PBrS core in the dewetted droplets is fully encapsulated by PS only when the bottom PS substrate thicknesses \( h_{\text{PS}} \) is greater than \( R_g \). Only partial encapsulation is observed when \( h_{\text{PS}} < R_g \). The Neumann contact angle after dewetting is also seen to increase with \( h_{\text{PS}} \). 272 Wang et al. investigated the dewetting of PS on both low and high viscosity PMMA films \( (\eta_{\text{PMMA}}) \). On a high \( \eta_{\text{PMMA}} \) bottom layer, the dewetting speed is found to be constant and independent of the PS layer thickness. In contrast on a liquid like PMMA layer \( (\eta_{\text{PMMA}}) \), the radius of the dewetted holes grows as \( t^{0.2} \), \( (t \text{ is the annealing time}) \), and depends on the thickness of both the layers. 274 With a PVP/PS bilayer coated on a silicon wafer, Kang et al. observed a layer inversion during dewetting as a higher surface energy PVP preferentially wets the silicon substrate and thus fills up the holes created in the PS film and spreads along the substrate, dislodging preferential and controlled adsorption of protein molecules on a surface. 279

As bilayers are extremely sensitive to initial conditions, accurate simulations play a crucial role in predicting the morphology, the evolution pathway and more importantly, the morphology of the interface during and after dewetting, which cannot be directly visualized using real space imaging techniques. 286–288 Bandyopadhyay et al. theoretically showed that a likely transition from the squeezing and bending modes at later times can occur when the film thicknesses either correspond to the minima of the dominant growth rate or when switching between the high- and low-wavenumber regimes occurs. 287 They also presented the short- and the long-time dynamics, interfacial morphologies, and the rupture and dewetting pathways based on nonlinear simulations, which suggests that over longer durations the intermolecular and viscous forces can profoundly modify the initial mode of instability and its growth rate, resulting in complex later stage morphologies such as embedded droplets, inversion of top and bottom phases, and encapsulation of one layer by the other film. 288

When a polymer bilayer is dewetted on a topographically patterned substrate, it is possible to have a variety of exciting structures such as an array of core–shell droplets, an array of droplets under an intact top layer, aligned undulating threads, and co-existing ordered droplet arrays of both polymers, can be obtained depending on the thickness ratio and the initial morphology of the bilayer. 289 Based on nonlinear simulations, the likely morphology of a polymer bilayer on chemically and topographically patterned substrates has been predicted by Bandyopadhyay and Sharma. 290,291 Their work provides a comprehensive understanding of the system and highlights the possibility of obtaining a variety of interesting and complex, dissipative patterns based on an interplay of various parameters such as pattern geometry, dimension, thickness and interfacial tension of both the layers, and substrate wettability. 290,291

Ding and coworkers have explored the evolution of a polymer bilayer with a topographically structured interface. 292–295 On a thick patterned PMMA layer, they observed two sequential events of capillary instability, which lead to PS stripes segregated on the PMMA mesas and PS threads confined in the PMMA trenches. 292 The kinetics of the capillary breakup is a strong function of the duty ratio and the viscosity ratio of the two polymers and is dominated by the property of the more viscous component. 293 When both the layers are thin, the PS (or PMMA) stripes confined within PMMA (or PS) trenches break up, either nucleated, out-of-phase, or without clear phase correlation depending on the geometry, residual layer thickness and molecular weight ratio.
between the two polymers.294 They observed a vertical pattern decay in dewetting of a nano-imprinted bilayer, and the formation of final structures in a direction orthogonal to that of the initial stripes, leading to partially ordered structures.295

2.6 Perspective on thin film dewetting

In this section we have presented a short overview on how research on spontaneous rupture, instability and pattern formation in thin viscous films has evolved over the last two decades. Though dewetting of simple liquids such as water or organics solvents was known for a long time, the use of a polymer by Gunter Reiter in 1992 as a model system for experimentally studying dewetting of a thin film revolutionised the field, with renewed interest. There are several advantages of using a polymer over a simple, regular liquid, as the evolution can be frozen at an intermediate stage by mere switching of temperature. The structures, at least during the timescales of experiments were absolutely stable, as evaporation, an inherent problem in any liquid, is completely eliminated in a polymer. The solid like frozen structures also paved the way for characterizing the dewetted features by techniques such as AFM and SEM, as well as the scattering based reciprocal space techniques, each one of which have given far more insight into the physics of the system than simple optical microscopy based observations.

Alongside novel and elegant experiments, theoretical developments in the field also matured with simulated predictions that could be directly compared with experimental observations. Despite the in-depth understanding in the field, certain ambiguities still remain, which we have highlighted in our discussion. For example, many groups have reported (and therefore, repeatability is unquestionable!) dependence of \( \lambda \) or \( N_m \) with \( h \) that is identical to theoretical predictions in pure spinodal dewetting, in much thicker films where nucleation seems to be the sole reason for rupture. Similarly, though theoretical predictions match with experimental findings rather well, even in terms of morphology, most of the models consider Newtonian behaviour of the polymer melt, which for long chain molecules is hard to accept. Another major issue that many researchers have not accounted properly is the confinement induced reduction of the \( T_g \) during actual dewetting, which is likely to have strong influence on the rupture timescale and dewetting velocity.

The ordering of the dewetted structures on the topographically patterned substrate is indeed a novel meso-patterning strategy, and offers much higher degree of morphology control and flexibility as compared to classical top down methods. Still it is unlikely that this approach will find more favour with users for nano-patterning over existing soft lithography methods, due to the sensitive nature of the final morphology under initial conditions and delicate experimental protocols. However, such a method can be indeed useful for functional materials for novel applications such as imaging, sensing, water harvesting, and sustained drug release, particularly exploiting the instability of bilayers which has the potential to fabricate embedded or submerged structures with definite interfacial architecture that is impossible to achieve by any existing top down method.

3. Category 2: contact proximity induced instability in thin elastic films

3.1 Elastic contact (EC) instability: theory

In this section, we review contact proximity induced instability observed in a soft solid film that exhibits room temperature elasticity (category 2).206–245 In contrast to category 1 instability involving dewetting, where the excess interfacial free energy within the film causes the instability, in the present case instability results due to an attractive interaction between the free surface of the film and another rigid surface (the contactor), when the two are in close proximity. Unlike category 1, where surface tension opposes the growth of instability, in a soft elastic film the role of surface tension is rather insignificant and the instability is opposed solely by the elasticity of the film. Further, in this case instability is associated with solid state deformation and does not involve any advective transport of material by flow or diffusion. Deformation of a thin elastic film confined between two surfaces is important in various settings such as adhesion, friction,206 peeling of a pressure sensitive adhesive,297 crazing behavior of glassy polymers,298 and interfacial bonding in composite materials.299 EC instability is distinct from instabilities in pre-stressed solid films engendered by the elasticity of the film itself,300 or due to large nonlinear plastic deformation.301 Despite strong morphological similarities, EC instability is completely different from the classical Saffman–Taylor instability observed in a Hele Shaw cell, where flow-driven fingering patterns form at a moving interface between two viscoelastic liquids.302 In EC instability, the destabilizing energy remains stored within the flexible matrix of the elastic film itself and once the contactor is withdrawn, the stored energy is released and the film surface restores back to its original flat morphology.303,311

The elastic strain energy per unit area of a deformed film surface \( (U) \) is given by:

\[
U \approx \mu h (\partial v/\partial x + \partial u/\partial z)^2
\]  
(7)

where, \( \mu \) is the elastic modulus, \( u \) and \( v \) are the components of the displacement field in the lateral \( (x) \) and the normal \( (z) \) directions, respectively.303,304 By considering the characteristic orders of the length scales as \( x \sim \lambda \) (instability length scale), \( z \sim h \) (film thickness) and \( v \sim \delta \) (vertical amplitude of the pattern) in eqn (7), in conjunction with the continuity equation \( \partial u/\partial x + \partial v/\partial z = 0 \), provides a scaling relation for the stored elastic energy due to the shear and normal deformations of the film surface as:

\[
U \approx \mu h \delta^2 (\lambda^{-1} + \lambda H^{-2})^2
\]  
(8)

It can be seen in eqn (8) that the energy penalty for deformation of the film surface increases for both very short \( (\lambda < h) \) and for very long \( (\lambda \gg h) \) wave undulations, and therefore the minimum energy configuration \( (\partial U/\partial \lambda = 0) \) is attained only when \( \lambda \approx h \). A numerical pre-factor close to 3 for the scaling relation \( (\lambda \approx 2.96h) \) is obtained based on detailed LSA.303–306 The analysis also shows that \( \lambda \) is independent of the elastic modulus of the film at the onset of instability as well as the surface tension of the contactor,303,304 which has been experimentally verified.311,330–334
The pre-factor may increase significantly to values higher than 3 in films thinner than \( \approx 1 \) \( \mu \)m due to the enhanced effect of surface tension.\textsuperscript{311} Nonlinear simulations based on complex energy minimization have been used to predict and understand the mechanism and pathways during the approach and de-bonding of a rigid contactor to/from a soft interface. Simulations also show the existence of an adhesion–debonding hysteresis, due to the energy barrier associated with the pinning of the metastable patterns with the contactor surface during debonding.\textsuperscript{306,307} Finite element based models have also been used to capture the nonlinear regimes of elastic instability.\textsuperscript{312,313}

### 3.2 Elastic contact instability: experiments

Experimentally, EC instability in thin films has been studied in three distinct geometries: (1) peeling a rigidly bonded convex or cylindrical contactor from the film, which is similar to the well known probe tack test geometry;\textsuperscript{314–321} (2) peeling a flexible contactor from one side of a flat film;\textsuperscript{322–329} and (3) bonding–debonding of a flat rigid contactor parallel to the film surface.\textsuperscript{311,330–332} In experiments with a rigidly bonded convex contactor, the film becomes unstable at a critical nominal strain as the contactor is detached under a constant tensile load and undulations appear along the circular contact line at the onset of instability.\textsuperscript{314–316} The perturbations become prominent with inward growth of the elastic fingers due to reduced lateral confinement at large strains. At higher tensile loads, a cohesive fracture results half way between the two contacting surfaces. The morphology of the patterns is strongly influenced by the extent of imposed confinement and the mode of cohesive failure can vary from simple interfacial fracture to cavitation in a fibrillated structure.\textsuperscript{315,316}

In peeling experiments with a flexible contactor, which typically is a microscope cover slip, the interfacial crack propagates in the direction of peeling, resulting in undulating elastic fingers at the crack front, which can be seen in Fig. 6A. The fingers form due to non-uniform deformation at the contact line caused by adhesive stresses, as spatially varying deformations correspond to a lower energy configuration for the system.\textsuperscript{322,323,337,328} The wavelength (\( \lambda \)) of the patterns varies linearly with \( h \), and is found to be independent of the shear modulus (\( G \)) of the film, the flexural rigidity (\( D \)) of the contactor, as well as the surface energy of the film and the substrate.\textsuperscript{322,323,328} However, the amplitude of the fingers (\( l_0 \)) reduce with increased rigidity of the contactor. The fingers become highly irregular when \( l_0 \) exceeds \( \lambda \), and tend to split, resulting in isotropic ripple-like structures (Fig. 6A).

Also, for a specific value of \( D \), there exists a critical \( h \) beyond which no meniscus instability is observed.\textsuperscript{322,323} In case the contactor is peeled from a film which has multiple incisions, the crack moves intermittently as the edges create crack-initiation barriers. The dynamics of crack propagation depends strongly on the depth, geometry and spacing of the incision patterns.\textsuperscript{325,326} The resistance to crack propagation leads to significant enhancement of fracture energy between the film and the contactor. This concept has led to the development of a new class of reusable pressure sensitive adhesives. The extent of adhesion can be enhanced by several orders in the presence of sub-surface liquid filled micro-channels. The additional crack arresting property of the channels can be attributed to capillarity induced surface stresses.\textsuperscript{329}

In the parallel configuration, the contactor is first brought in contact with the film and subsequently de-bonded, which allows tracking of the morphological transformation during a complete bonding–de-bonding cycle as a function of the inter-surface separation distance.\textsuperscript{311,330,332} The onset of instability during bonding is with the formation of isolated columns, which transform into bi-continuous labyrinths and then isolated holes with a progressive approach of the contactor (Fig. 6B, frames B1–B4).\textsuperscript{311,330} An exact opposite sequence with hysteresis in the separation distance is observed during de-bonding (Fig. 6B, frames B5–B8). Interestingly, \( \lambda \) remains nearly invariant across all morphologies due to the pinning of the initial instability structures to the stamp in a local thermodynamic metastable state.\textsuperscript{311} A soft flexible stamp however fails to cause any surface instability as it succumbs to the attractive inter-surface interaction, forming instantaneous conformal contact with the film surface.\textsuperscript{334}

### 3.3 Contact instability of the elastic bilayer and two interacting films

Additional controls over the pre-factor (\( R_E \)) in the scaling relation between \( \lambda \) and \( h \), which remains nearly constant at \( R_E \approx 2.96 \) in a single layer film, can be achieved by using an elastic bilayer comprising of two stacked elastic films with different shear moduli (\( \mu_1 \) and \( \mu_2 \); shear modulus of bottom and top layers respectively) and thicknesses (\( h_1 \) and \( h_2 \); thickness of bottom and top layers respectively) due to coupled deformation at the interface between the two layers.\textsuperscript{335–337} The magnitude of \( R_E \) is strongly influenced by the stacking order of the films. When a softer film is placed on top of a stiffer film, \( R_E \) assumes values lower than 3 and can be as low as 0.75 under specific conditions (Fig. 6C).\textsuperscript{335} This allows significant downsizing in pattern dimensions.\textsuperscript{335} A stiffer film on top of a softer film results in an increase of \( R_E \) to values higher than 3, as the horizontal deformation at the interface results in an effective slip-like effect for the top film.\textsuperscript{335,337}

When two soft elastic films with dissimilar shear modulus approach each other, a co-operative instability mode at a common \( \lambda \) evolves, which has a non-linear coupling between the vertical and parallel displacements in both the films.\textsuperscript{338–341} Nonlinear simulations show that \( \lambda \) of the patterns increases with increased compressibility of the film and is dominated by the film with higher compressibility. In the event the two interacting films having equal shear moduli, \( \lambda \) depends on the relative thicknesses of the films.\textsuperscript{340} In case the thicknesses of the films are substantially different, the overall \( \lambda \) is found to be intermediate between \( \lambda \) of each film had they been in contact with a rigid contactor.\textsuperscript{340} For highly compressible film, the instability is suppressed in favour of a near conformal contact.\textsuperscript{338}

### 3.4 Elastic contact lithography

Elastic contact lithography (ECL) is an approach that aims to align the random instability patterns by imposing lateral confinement.\textsuperscript{331–333,342–345} Strategies adopted in this regard include: (1) the use of a topographically patterned stamp,\textsuperscript{331–333,342,345}
(2) using a topographically patterned substrate,343,344 and (3) shearing of a flat stamp while it is in contact with the film.331,332 ECL has been implemented in an elastic bilayer to derive the advantages of feature dimension miniaturization as well.345 The key advantage of ECL over existing soft lithography methods is the possible creation of patterns with distinct morphologies by controlling the commensuration between the $l$ of the film and the $l_P$ of the stamp/substrate, along with their in situ manipulation, reconfiguration and potential ability to create structures on demand.331,332,345

Fig. 7 shows the morphological evolution sequence when a grating stamp approaches a soft elastic bilayer. The onset of instability is with the formation of aligned columns (Fig. 7A), which transforms to a positive replica of the stamp (Fig. 7D), through various intermediate stages. Further approach of the contactor beyond the stage of a positive replica results in the appearance of periodic undulations along the periphery of each stripe (Fig. 7E, inset) which eventually bridge across adjacent stripes, forming bifurcated 2D structures (Fig. 7F and G) comprising an array of pico-litre beakers. Formation of such ordered 2D structures takes place only when $\lambda \approx \lambda_P$ and has been observed in single layer elastic films,331 metal coated thin elastic films,342 as well as thin films of hydrogels.333 Similar ordered 2D patterns have also been obtained using a grating substrate and a flat contactor, where the influence of the substrate “bleeds” through the film to the free surface, resulting in ordered, aligned patterns.345,346 In case there is a mismatch between $\lambda$ and $\lambda_P$, the film rather faithfully adheres to the instability length scale corresponding to 3 times the film thickness, paving the way for possible fabrication of structures with various duty ratios.331 The patterns are made permanent by UV ozone exposure which results in a stiff crust layer that prevents the relaxation of the film even after withdrawing the contactor. Patterns can also be aligned by shearing a flat stamp while in contact with the film in a specific direction, thereby transforming the random labyrinths into aligned stripes.331

3.5 Perspective on elastic contact instability
In this section we presented a class of instability that is specific to soft solid films that exhibit room temperature elasticity. The basic theoretical understanding of the genesis of instability is rather well understood. However the precise origin of the bonding–debonding hysteresis, additional stresses arising within the film matrix during debonding as a consequence of stretching, and whether the modulus of the film in any way influences the extent of hysteresis are yet to be fully resolved. From the standpoint of patterning, ECL has great potential to become a true beyond master patterning technique, where the
4. Category 3: external field mediated instability

In this section we review category 3 instability engendered by the application of an externally applied force field such as an electric field, or a thermal gradient, or in some rare cases, triggered by mere proximity induced effects itself! This type of instability is observed in both glassy as well as elastic films. A higher strength of the external field and a long range of electrostatic interactions can destabilize much thicker (~ few hundred nm) films following this approach, as compared to category 1 instability setting.

4.1 Electro-hydrodynamic instability (EHD)

The effect of an external electric field on the surface of a viscous film was first shown in 1897 by Swan. However, it was quite recently that EHD instabilities were utilized for patterning a polymer thin film, where an electric field is applied across a polymer film sandwiched between two electrodes separated by a spacer, in a capacitor geometry. The applied voltage between the two electrodes results in an excess electrostatic pressure \( p_{EL} \) at the free surface of the film and amplifies the interfacial capillary fluctuations in the direction of the field. Based on minimization of stored energy within the capacitor at a constant applied voltage \( U \), an expression for \( p_{EL} \) can obtained as:

\[
p_{EL} = -\varepsilon_0 \varepsilon_p (\varepsilon_p - 1) E_p^2
\]

where \( \varepsilon_0 \) is the dielectric vacuum permittivity, \( \varepsilon_p \) is the dielectric constant of the polymer and \( E_p \) is the strength of the electric field in films. The corresponding dispersion relation in a system dominated by electrostatic forces is given as:

\[
\tau = -\left(\frac{h_0^3}{3\eta}\right) [q^4 + q^2 (p_{EL}/\partial h)]
\]

where \( h_0 \) is the initial film thickness, \( \eta \) is the viscosity and \( q \) is the wavevector. A dependence of \( \tau \propto q^2 \) is a clear signature of a dissipative system. The necessary condition for the amplification of the fluctuations is \( \tau > 0 \), which becomes possible only when \( \partial(p_{EL})/\partial h < 0 \). The expression for the corresponding wavelength \( \lambda \) of the fastest growing mode is obtained as:

\[
\lambda = 2\pi \sqrt{\frac{\gamma \varepsilon_p d - \varepsilon_p - 1) h_0^3}{\varepsilon_0 \varepsilon_p (\varepsilon_p - 1)^2 U^2}} = 2\pi \sqrt{\frac{\gamma U}{\varepsilon_0 \varepsilon_p (\varepsilon_p - 1)^2} E_p^{-3/2}}
\]

In experiments, early stages of EHD instability is manifested with the appearance of surface undulations (Fig. 8A). The amplitude of the fluctuations grow with time in the direction of the applied field, eventually leading to the formation of columns that span the entire gap spacing \( d \) between the top electrode and the film (Fig. 8B). The columnar configuration corresponds to lowering of the total electrostatic energy of the capacitor compared to an initially flat film with an air gap. The extent of ordering of the columns depends largely on the fill factor \( f(h/d) \), in addition to field strength and surface tension. Columns with perfect hexagonal symmetry and denser packing results at higher values of \( f \) due to a higher degree of electrostatic repulsion between equally charged undulation peaks (Fig. 8C). For \( f > 0.5 \), the film remains partially interconnected even after column formation and final morphology is strongly influenced by later stage ripening. At very high \( f (> 0.75) \) coalescence of columns leads to phase inversion, resulting in cavities in a continuous polymer matrix.

Additional ordering of the patterns can be achieved by using a topographically patterned top electrode or a patterned substrate. As a result of periodic spatial variation in...
...the electrostatic field strength over the film surface, the emerging patterns evolve along the contours of the stamp/substrate. Depending on $f$ and the relative magnitudes of $\lambda_p$ and $\lambda$, the final patterns either comprise an array of aligned pillars (Fig. 8D) or a positive replica of the stamp (Fig. 8E). On the other hand, a nucleated instability under a single heterogeneous patch is seen to result in a rosette of columns along a circle with radius $r \approx 2\lambda$ (Fig. 8F). Such an unique morphology is attributed to the suppression of the nearest neighbor undulations due to the flow of the polymer towards the point of nucleation, which allows the second order effects to amplify, resulting in the formation of a rosette of columns at $r \approx 2\lambda$. EHD lithography has been utilized for patterning low viscosity photo-curable polymers like epoxy, vinyl ether, acrylate, and thiol–ene, and sol gel utilized for patterning low viscosity photo-curable polymers like dewetted patterns. On the other hand, a spatially modulating narrow size distribution and spatial ordering, resembling field results in the formation of isolated polymer droplets with a radius.

A thin polymer film can also be destabilized by an in-plane or a spatially modulating electric field. In plane the electric field results in the formation of isolated polymer droplets with a narrow size distribution and spatial ordering, resembling dewetted patterns. On the other hand, a spatially modulating field exhibits two distinct regimes with a clear boundary that is defined by the dimensionless field strength ($\tau$) and the dimensionless lateral field modulation ($c$) in the phase space (Fig. 8G). While the first regime exhibits stable surface undulations with finite amplitudes matching the periodicity of the imposed field, in the second regime the film breaks up into pillars localized around the region of maximum field strength. A finite conductivity can lead to patterns with smaller wavelengths and faster growth rates in leaky dielectric liquids. Extremely interesting to point out that Chou and co-workers observed the formation of pillars in polymeric thin films in very close proximity to another rigid substrate, without the application of any electric field. The mechanism is scientifically intriguing as the key driving force for the appearance of the structures is believed to be the internal localized electrical field generated between the con looseness and the viscous film. The generation of the electric field is attributed to the image charge-induced electro-hydrodynamic-instability (ICE) model. In this method, known as Lithographically Induced Self Assembly (LISA), Rayleigh–Benard instability due to thermal convection, Benard convection driven by surface tension, surface charges accumulated on the film and the image charges on the contactor are argued to determine the final pattern morphology. The feature size can be minimized by filling the space between the contactor and the film by a liquid, as this reduces interfacial tension. Further, time resolved experiments have shown that the columns appear in a sequential manner, which is in clear contrast to elastic contact or EHD instability where the entire film evolves concurrently. The pillar forming cascade in LISA is attributed to an in plane variation of the pressure gradient which is maximum at the corners below the stamp and is higher along the edges, where the columns appear first.

4.2 Electric field induced patterning of polymer bilayers

EHD instability in a thin polymer bilayer has been investigated in two distinct configurations: without and with air gap...
between the film and the contactor. In case there is no air gap, the growth rate of the instability is much faster and the feature size reduces significantly due to reduced interfacial tension.363,364 On the other hand, in the presence of an air gap, either of the film–film or the film–air interfaces become unstable preferentially, resulting in the formation of hierarchical structures that exhibits a combination of two independent characteristic length scales.365–368,372–376 Generally, the film–film interface is slow to evolve due to higher viscous damping compared to the film–air interface.365 Depending on the strength of the field, it’s temporal modulation as well as the stacking order of the polymers, distinct morphologies are observed.365 A strong field favors the formation of columns as the evolution is dominated by the electrostatically amplified surface waves.365,366

In contrast, a weak field allows dewetting of the top layer before the onset of electrostatic instability.365,377,378 Temporal modulation of the electric field also significantly influences the final pattern morphology. The onset of instability is with the formation of PS columns in a PS–PMMA bilayer, if the electric field is applied ahead of softening of the film.366 The columns deform the bottom PMMA layer at the film–film–air contact line and induces a secondary instability which engenders the flow of PMMA around the periphery of the pre-existing PS columns, eventually resulting in an array of ordered columns with core–shell morphology (Fig. 9A).366 On the other hand, if the film is initially softened, the PS film dewets on an intact PMMA under layer initially. Subsequently, the PS droplets are stretched towards the top electrode by the electric field, forming columns.367 The deformed PMMA meniscus shows fingering instability around each PS column. The edge of the fingers climb along the periphery of the PS columns, forming narrow strands surrounding the PS core.367 Preferential removal of the PS core results in an unique PMMA cage (Fig. 9B), something that can never be obtained by any lithography.367 In case the higher dielectric PMMA film is placed over the PS film with a lower dielectric constant, the electrostatic forces acts upwards at the PMMA–air interface and downwards at the PMMA–PS interfaces, which in combination with dewetting results in a novel structures such as the PS core surrounded by the PMMA sheath.368

4.3 Electric field induced patterning in visco-elastic thin films

EHD instability is also observed in visco-elastic and purely elastic thin films.374–381 Similar to EC instability, EHD instability in an elastic thin film has been investigated in both peel configuration,377,378 and parallel electrode geometry.374,375,380,381 In the first case, depending on the stiffness of the film, three distinct types of shape changes along the contact zone is observed upon application of the electric field. In stiffer films, the applied field appreciably decreases the amplitude (δf) of the initial finger patterns above a critical voltage (Vc), resulting in a nearly flat, featureless edge at higher voltages (inset of Fig. 10A2).

In films with intermediate stiffness, a rapid increase in δf takes place beyond Vc, with concurrent multiple scissions at the elongated finger tips (Fig. 10A3). In contrast, in films with even lower stiffness, the fingers break down into an array of pillars (Fig. 10A4).377,378 The fingers reappear upon switching off the electric field in the first case, due to a purely elastic nature of the film. In contrast the morphological changes are permanent in the latter two cases due to enhanced viscous dissipation from the film.377,378

In the parallel electrode configuration, an array of columns with hexagonal closed packing is observed upon application of the electric field (Fig. 10B),380,381 the morphology of which is similar to that observed in a purely viscous film.347 In films with lower levels of elasticity, there is no Vc and in this regime, λ varies rather strongly with the visco-elasticity of the film (Fig. 10C1).380 In contrast, in stiffer films, instability sets in only when the applied voltage exceeds a critical Vc. In such films, λ does not depend on the precise rheology of the film and exhibits a nearly linear scaling λ ≈ 4h with film thickness (Fig. 10C2). Fig. 10C3 shows a clear transition of λ from long-wave in a purely viscous film to short-wave in a purely elastic film, over a narrow range of elastic modulus.380 Pattader et al. showed that temporal modulation of the applied electric field also influences the pattern morphology in weakly crosslinked films, due to the appearance of secondary and tertiary structures, resulting in hierarchical patterns, which can be observed in Fig. 10D.381

4.4 Thermal gradient induced patterning

A thermal gradient applied across a film can also destabilize it, resulting in meso-scale features.382–389 The experimental arrangement is nearly identical to that used in LISA, except in this case the contactor and the film is maintained at two distinct temperatures. Rearrangement of a flat film into columns spanning the two plates maximizes the heat flux. It is important to highlight that though a temperature gradient exists, neither Rayleigh–Benard or Benard–Marangoni convection effects are strong in case of a thin polymer film with high viscosity.

Rather, heat transfer across the polymer film with air gap is attributed to a diffusive mechanism, with molecular vibration being responsible for the transport of heat within the polymer film.382 Depending on the fill factor f either columnar (lower f, Fig. 11A)
or striped morphology (higher $f$, Fig. 11B) is obtained.\textsuperscript{383} The patterns can further be aligned with a topographically patterned top plate, examples of which are shown in different frames of Fig. 11C–F.\textsuperscript{382}

4.5 Perspective on external field mediated instability

The key advantage of EHD instability in patterning lies in its ability to create ordered structures with a flat, featureless stamp as well as its rather material invariant nature. Scientifically this phenomenon is extremely fascinating and often in conjugation with dewetting, is capable of extremely novel structures such as cages which can be ideal candidates for drug release and other nano-biotechnology applications. However, the experiential procedure is complicated, and reproducibility is certainly an issue. This is in fact a reason why unlike dewetting, which has been experimented by a large number of groups worldwide, publications on EHD instability still comes only from a few selected groups. Steiner has explored and already reported most of the relevant features of EHD in a viscous film. However issues related to EHD instability in elastic and VE films are yet to be understood fully. For example, it is seen that the columns remain intact even after switching off the electric field in an elastic film. However, in EC instability, the structures fade away once the contactor is withdrawn. Despite the physical cross-linking of the polymer chains in the film, what precisely allows the columns to remain stuck to the top electrode is an unresolved scientific issue. Even in a viscous film, whether the presence of conducting nano-particles in trace quantities will influence the instability or not can be another fascinating problem. One may take clues from EHD experiments and can...
see the effect of an external magnetic field in polymer films containing magnetic nano-particles.

5. Conclusions and perspective

The review presented here provides an illustrative commentary about the progress and recent developments on the rich phenomenon of surface instability and morphological evolution of an incompressible visco-elastic thin film. The key emphasis of the review has been to discuss the conditions under which instability mediated structures can be ordered, often in conjugation with some top down lithography methods, for the possible fabrication of novel structures spanning over large areas that are difficult to realize with conventional top down techniques. We have discussed how historically research on meso-mechanics of polymer thin films has progressed following three distinct routes, depending on the nature of the confining field and to some extent, the rheology of the film. To facilitate discussion, we have categorized the instabilities in three distinct regimes. At this point we would like to highlight the fundamental difference between spontaneous instability (category 1) with both contact proximity induced (category 2) and external field mediated (category 3) instabilities. In the first case, the morphological evolution is associated with lowering of the free energy of the system. In contrast, when an external field is applied, the system is intrinsically out of equilibrium and an exact equivalent of the Gibbs’ free energy is difficult to formulate. Consequently, the morphological evolution in the latter case is associated with the maximization of the flux. 390

At this point we would like to highlight a relatively new formulation by Sarkar and Sharma, where based on linear stability analysis it is argued that these apparently distinct categories of instabilities are manifestation of generic instability in a soft visco-elastic thin film. 314 It is seen that the nature of the instability (shortwave or long-wave) of a viscoelastic films, in both the wetting and adhesive configurations, is determined by a parameter $\gamma/\mu h$. One limiting case is a confined purely elastic film, for which $\gamma/\mu h < 10^{-2}$, which corresponds to $h_{km} = 2.12$ and $\lambda = 2.96\theta h$. On the other extreme, in a purely viscous wetting film $\gamma/\mu h$ is $>1$ and the critical wavelength acquires a long-wave nature. 314 A gradual transition of the nature of the instability length scale from long-wave to short-wave with enhanced visco-elasticity has been nicely captured by Arun et al. 391 in the context of EHD of a visco-elastic thin film. It strengthens this argument of visualizing the apparently different settings as different limiting cases of a generic instability in soft visco-elastic thin films. It is clearly seen that progress in this field has been made based on the combination of robust theoretical modeling and simulations, along with carefully performed experiments. Simulations greatly reduce the experimental efforts, and nicely capture regime cross-overs which are difficult to obtain based on pure experiments.

We have added a perspective for each theme, which highlights some of the yet unresolved issues for each theme, and have specifically mentioned the practical utility of instability mediated fabrication in nano-patterning. This review adequately highlights the advantages of instability mediated patterning, in terms of richness of physics as well as the flexibility the methods offer in terms of morphology control, which allows possible fabrication of various different structures and are not mere negative replicas of stamp features as well as their in situ modulation based on controlling the initial conditions. However, due to delicate experimental protocols and sensitivity towards initial conditions, bulk nano-fabrication of instability mediated structures might take some time before it reaches the

![Fig. 11](image-url) (A and B) Instability structures in polymer films exposed to laterally homogeneous temperature gradients by sandwiching between two flat plates at different temperatures. (A) The columnar structure in a 106 nm thick PS film, gap between plates ($d = 448$ nm, plate temperatures 170 °C ($T_1$) and 124 °C ($T_2$) respectively; (B) Stripe patterns in a 100 nm thick film with $d = 202$ nm, $T_1 = 170$ °C and $T_2 = 133$ °C. (C–E) Pattern replication in temperature-gradient driven capillary instability with a patterned top plate on the surface of a 106 nm thick PS film with various plate spacings ($d = 160$ nm in (C) to $d = 220$ nm in (E)), due to which the replicated hexagonal arrays have periodicity of 2 μm, 4 μm and 10 μm respectively. (F) A 500 nm cross-hatched pattern. AFM images in the insets show the structure of the master and the replicated pattern, respectively. Reproduced with permission from ref. 393. Copyright 2003 Wiley-VCH.
level of commercialization, particularly for implementation of beyond the master patterning concepts.397–400

We would like to remind the readers that instability in a thin film is observed in many other settings, but in order to keep the review focused, only instability observed with homo polymer thin films are discussed in this article. Many examples that involve phase segregation like polymer blends, block copolymers, and evaporation induced assemblies are not included. As a final summary, instability mediated patterning indeed seems to be a promising approach for the fabrication of novel meso- and nano-structures in a rapid, cost effective manner. Future progress in this area will involve structure formation in functional polymers with more complicated molecular architecture and their potential integration into devices such as sensors, solar cells, and biochips to name a few.

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